

# Street Magician

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            2 seconds  
Memory limit:         256 megabytes

While visiting the farmers' market, Busy Beaver stops to watch a street magician. The magician presents a row of  $N$  boxes, holding  $M$ -bit nonnegative integers  $a_1, a_2, \dots, a_N$ , where  $0 \leq a_i < 2^M$  for all  $1 \leq i \leq N$ .

The magician magically sorts the boxes into non-decreasing order by a series of magic swaps. In a single magic swap, the magician chooses an index  $i$  ( $1 \leq i < N$ ) such that the binary representations of  $a_i$  and  $a_{i+1}$  differ by exactly one bit, and swaps  $a_i$  and  $a_{i+1}$ .

Watching the performance, Busy Beaver wonders about the limits of this trick. Out of all  $2^{MN}$  possible initial values of  $a_1, a_2, \dots, a_N$  in the boxes, how many of them can be sorted into non-decreasing order using magic swaps? Since this number may be large, Busy Beaver is content with finding it modulo  $10^9 + 7$ .

## Input

The first and only line of input contains two integers  $N$  and  $M$  ( $1 \leq N, M \leq 50$ ).

## Output

Output a single integer: the number of sequences that can be sorted using magic swaps, modulo  $10^9 + 7$ .

## Scoring

There are five subtasks for this problem.

- (10 points):  $1 \leq N, M \leq 5$ .
- (20 points):  $1 \leq M \leq 4$ .
- (10 points):  $1 \leq M \leq 10$ .
- (10 points):  $1 \leq M \leq 15$ .
- (50 points): No additional constraints.

## Examples

standard input	standard output
3 2	44
50 1	898961331
10 10	649370314

## Note

In the first sample, one sequence that can be sorted using magic swaps is  $[a_1, a_2, a_3] = [3, 1, 2]$ , as follows:

1. Choose  $i = 1$ . Note that  $a_1 = 3$  and  $a_2 = 1$  differ by exactly one bit, so this is a magic swap. The sequence becomes  $[1, 3, 2]$ .
2. Choose  $i = 2$ . Note that  $a_2 = 3$  and  $a_3 = 2$  differ by exactly one bit, so this is a magic swap. The sequence becomes  $[1, 2, 3]$ , which is in non-decreasing order.

Out of the  $2^{3 \cdot 2} = 64$  initial sequences, 44 of them can be sorted using magic swaps.