

## Problem I. Composition of Polynomials

Input file: polycomp.in  
 Output file: polycomp.out  
 Time limit: 2 seconds (3.5 seconds for Java)  
 Memory limit: 256 mebibytes

You are given polynomials  $f(x)$ ,  $g(x)$ ,  $h(x)$  over field  $\mathbb{Z}/2\mathbb{Z}$ .

Find the polynomial  $f(g(x)) \bmod h(x)$ .

### Input

The first three lines of input contain polynomials  $f$ ,  $g$  and  $h$ , one per line. Each polynomial  $p$  is described as  $n p_0 p_1 p_2 \dots p_n$  ( $1 \leq n \leq 4000$ ,  $p_i \in \{0, 1\}$  for all  $i$ , and  $p_n = 1$ ). The polynomial  $p(x)$  is then equal to  $p_0 + p_1x + p_2x^2 + \dots + p_nx^n$ .

### Output

Print the resulting polynomial in the same format.

If the answer is the null polynomial, print it as "0 0".

### Examples

polycomp.in	polycomp.out
5 0 1 0 1 0 1 2 1 1 1 4 0 1 1 0 1	1 1 1
2 1 1 1 3 0 0 1 1 4 1 0 1 0 1	3 1 0 0 1

### Note

Let us recall some definitions.

The field  $\mathbb{Z}/2\mathbb{Z}$  is a set of two elements 0 and 1 where results of addition, subtraction, multiplication and division are remainders modulo 2 of the corresponding results for ordinary integers.

A polynomial  $f(x)$  over this field is an expression of the form  $f_n \cdot x^n + f_{n-1} \cdot x^{n-1} + \dots + f_1x + f_0$ , where coefficients  $f_n, \dots, f_0$  are integers from  $\mathbb{Z}/2\mathbb{Z}$ , and the variable  $x$  can hold values from  $\mathbb{Z}/2\mathbb{Z}$  too. The maximum integer  $n$  such that  $f_n \neq 0$  is called the degree of the polynomial  $p(x)$ .

Polynomials  $a(x) = \sum_k a_k x^k$  and  $b(x) = \sum_k b_k x^k$  are equal if  $a_k$  и  $b_k$  are equal for all  $k$ .

Addition and subtraction of polynomials are performed component-wise:  $a(x) \pm b(x) = \sum_k (a_k \pm b_k) \cdot x^k$ .

The product of polynomials  $a(x)$  and  $b(x)$  is  $c(x) = \sum_k c_k x^k$  where  $c_s = \sum_{t=0}^s (a_t \cdot b_{s-t})$ .

Polynomials can be divided by each other. For a non-null polynomial  $b(x)$ , we say that  $a(x)/b(x) = q(x)$  and  $a(x) \bmod b(x) = r(x)$  if  $q(x) \cdot b(x) + r(x) = a(x)$  and the degree of  $r(x)$  is strictly less than the degree of  $b(x)$ . It can be shown that  $q(x)$  and  $r(x)$  are uniquely defined.

Composition  $a(b(x))$  is the polynomial  $\sum_k a_k (b(x))^k$  where the power of a polynomial is defined via multiplication:  $(b(x))^0 = 1$ ,  $(b(x))^1 = b(x)$ ,  $(b(x))^p = b(x) \cdot (b(x))^{p-1}$  for  $p > 1$ . To find the coefficients, expand the expression and sum the coefficients for the same powers of  $x$ .