

# Huge Segment Tree

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            2 seconds  
Memory limit:         1024 megabytes

An interval of integers is considered *segment-tree-like* if the following condition holds:

- The interval that can be expressed as  $[2^i j, 2^i(j+1))$  ( $0 \leq i \leq K, 0 \leq j < 2^{K-i}$ ) with some integers  $i, j$ .

For a pair of integer  $(l, r)$  that satisfy  $0 \leq l < r \leq 2^K$ , it can be proven that it is possible to express the interval  $[l, r)$  as the union of segment-tree-like intervals. We denote the minimum numbers of intervals required as  $f(l, r)$ .

For  $k = 1, 2, \dots, 2K - 2$ , solve the following problem:

- Find the numbers of pairs of integers  $(l, r)$  ( $0 \leq l < r \leq 2^K$ ) such that  $f(l, r) = k$ , modulo 998244353.

## Input

The input is given from Standard Input in the following format:

$K$
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- $K$  is an integer.
- $2 \leq K \leq 5 \times 10^5$

## Output

Print the answer to the problem when  $k = 1, 2, \dots, 2K - 2$  in this order.

## Examples

standard input	standard output
3	15 14 6 1
5	63 110 132 114 70 30 8 1
10	2047 4975 10896 21772 38360 58724 77184 86312 81448 64324 42112 22576 9744 3304 848 155 18 1

## Note

In the first example, when  $k = 4$ ,  $f(l, r) = k$  holds only when  $l = 1, r = 7$ , so 1 is the output.