

Majority and Permutation

Input file: **standard input**
Output file: **standard output**
Time limit: 2 seconds
Memory limit: 1024 megabytes

You are given an integer sequence (A_1, A_2, \dots, A_M) consisting of odd numbers between 1 and $2N - 1$ (inclusive).

Find the number of permutations $P = (P_1, P_2, \dots, P_{2N})$ of $(1, 2, \dots, 2N)$ that satisfy the following condition, modulo 998244353.

- There exists a binary string S of length $2N$ consisting only of 0 and 1 that meets all of the following conditions:
 - The frequencies of 0 and 1 in S are exactly N each.
 - For each $i = 1, 2, \dots, M$, in the $1, 2, \dots, A_i$ -th characters of S , the most frequent character is 0.
 - For each $i = 1, 2, \dots, M$, in the P_1, P_2, \dots, P_{A_i} -th characters of S , the most frequent character is 0.

Input

The input is provided in the following format from standard input:

N M A_1 A_2 ... A_M

- All inputs are integers.
- $1 \leq M \leq N \leq 10^5$
- $1 \leq A_1 < A_2 < \dots < A_M \leq 2N - 1$
- A_i is odd.

Output

Print the answer on a single line.

Example

standard input	standard output
2 2 1 3	14

Note

For example, if $P = (2, 1, 3, 4)$, then $S = 0011$ satisfies all three conditions.

On the other hand, if $P = (4, 3, 2, 1)$, there is no string of length 4 that satisfies all three conditions.